

Energy

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Work

- Energy needed to enact a force through some displacement
- Measured in Joules (J)
 - $W = \text{force parallel (to displacement)} * \text{displacement}$ or $fd(\cos\theta)$
 - Assume force is constant
 - Specify if the object is doing the work or if it is having work done on it
 - Specify what force is doing the work

What is Energy?

- Energy is the ability to do stuff
- Energy is a scalar quantity (no direction)
- Energy is conserved, meaning that it cannot be created or destroyed
- Measured in Joules (J)

Types of Energy

- Kinetic Energy
- Potential Energy
 - Gravitational Potential Energy
 - Elastic Potential Energy
- Nuclear
- Thermal
- Chemical

Potential Energy

- How much energy an object has by virtue of its position or configuration
- Can only be defined for conservative forces
 - Gravitational: mgh
 - Elastic: $\frac{1}{2}(k)(X^2)$

Gravitational potential energy

- The change in potential energy that has physical meaning
- The work done by gravity depends only on the height, NOT ON THE PATH YOU TAKE!
- $PE_g = mgh$ = weight x height
- Example: A brick that has a mass of 20 kg is lifted 3m above the ground, what is the potential Energy of the brick?

$$PE_g = mgh = 20\text{kg} \times 9.81\text{m/s}^2 \times 3\text{m} = 588.6 \text{ J}$$

Elastic Potential Energy

- Spring Force: **Hooke's Law**
- $F_s = -kx$ (k is spring constant \Rightarrow measure of stiffness)
- This value is **NEGATIVE** because force is opposite displacement (“restoring force”)

❖ $PE_e = \frac{1}{2} kx^2$

- ❖ Example: The spring constant of one spring is 220N/m, and the spring has a potential energy of 40J, How much is the spring stretched?

$$PE_e = \frac{1}{2} kx^2 \quad 40J = \frac{1}{2} (220N/m)(x^2) \quad x = 0.60m$$

Conservative Forces

- Forces in which only the initial and final positions are important
 - Path of the object doesn't matter
 - Ex: Gravity, spring, elastic

Non-conservative Forces

- Forces in which the path of the object matters in addition to the initial and final positions of the object
 - Potential Energy can't be defined for non-conservative forces
 - Ex: Friction, air resistance, tension, applied force

Dissipative Forces

- Forces that reduce the total amount of mechanical energy when an object is in motion
 - Ex: Friction

Energy Transformation

- Potential energy at the beginning equals the kinetic energy at the end
- Ex: Stone in freefall
 - At the top the energy is all potential
 - Mid-air the energy is both potential and kinetic
 - Just before the stone hits the ground the energy is only kinetic

Work-Energy Theorem

- Net work = conservative forces + non-conservative forces
(change in kinetic energy)
- Include all forces acting on the system
 - Conservative forces = change in potential energy
 - Non-conservative forces = change in kinetic energy + change in potential energy

Mass Energy

- Einstein: “All mass have intrinsic, internal energy just by virtue of their existence”.
- $E=mc^2$
- c = the speed of light = 3.00×10^8 m/s

Power

- The rate at which the work is done
- OR the rate at which energy is transformed
- $P=W/t$
- Unit is Watts (W)

Machines

- Simple machines: device that use only the forces directly applied and accomplish their task with a single motion
- Input vs. Output
- $W_{in} = W_{out}$
- Mechanical Advantage: the ratio of output force to input force
- $MA = F_{out} / F_{in}$

Lever

- Includes a stiff structure (the lever) that rotates around a fixed point called the fulcrum
 - Mechanical Advantage of lever = $F_{out}/F_{in} = L_{in}/L_{out}$
 - L = Length of the lever, F = Force

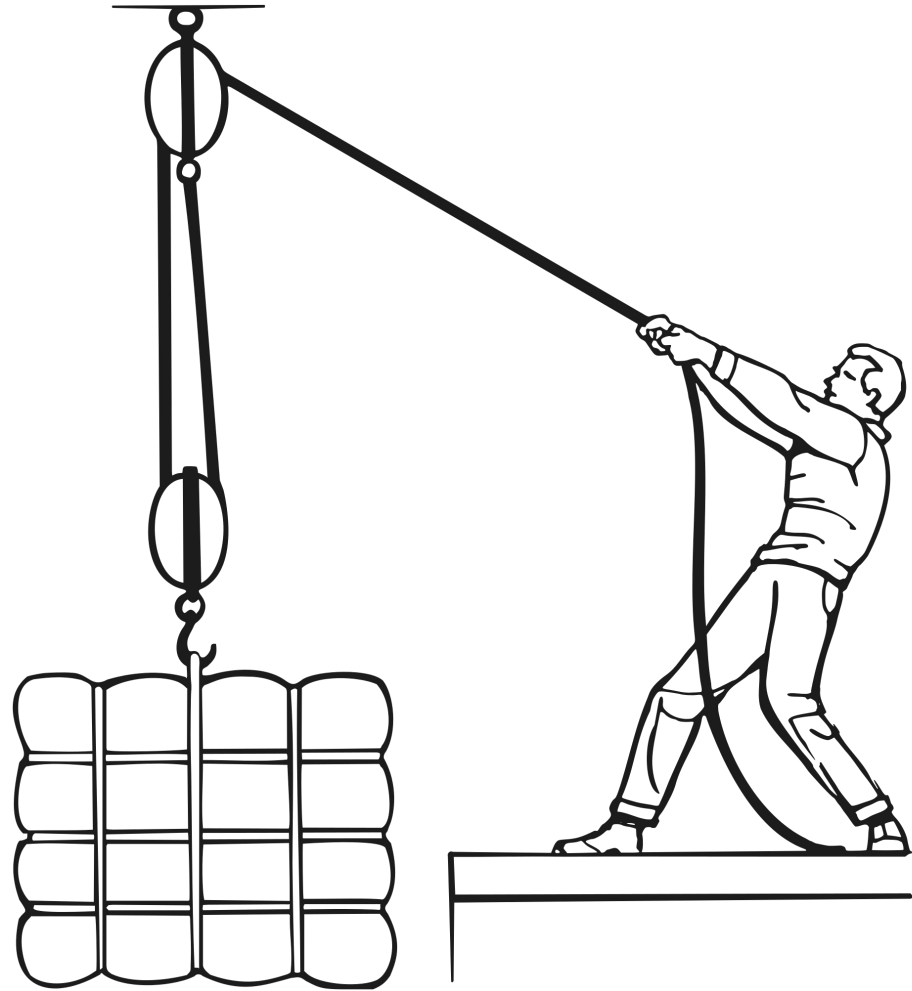
Ramps

- Draw problem with given forces/measurements
 - $MA = \text{Length of ramp} / \text{height of ramp}$



Pulleys

- Like levers and ramps, pulleys sacrifice displacement to achieve a greater force
 - MA is shown by how many ropes there are



Efficiency

- $\text{Output WORK} / \text{Input WORK} * 100 = \% \text{ efficiency}$
- Always smaller than 1

Practice Problem

- A roller coaster car of 150 kg starts on a hill that is 30m tall and it moves at 20m/s. It must travel down the first hill and up a second hill that is 10m tall.
 - What is the potential energy at the top of the starting hill?
 - What is the velocity at the bottom of first hill?
 - What is the kinetic energy at the bottom of the second hill if the velocity changes to 25m/s?



Answers

- 44,145 J
- 31.4 m/s
- 46,875 J

